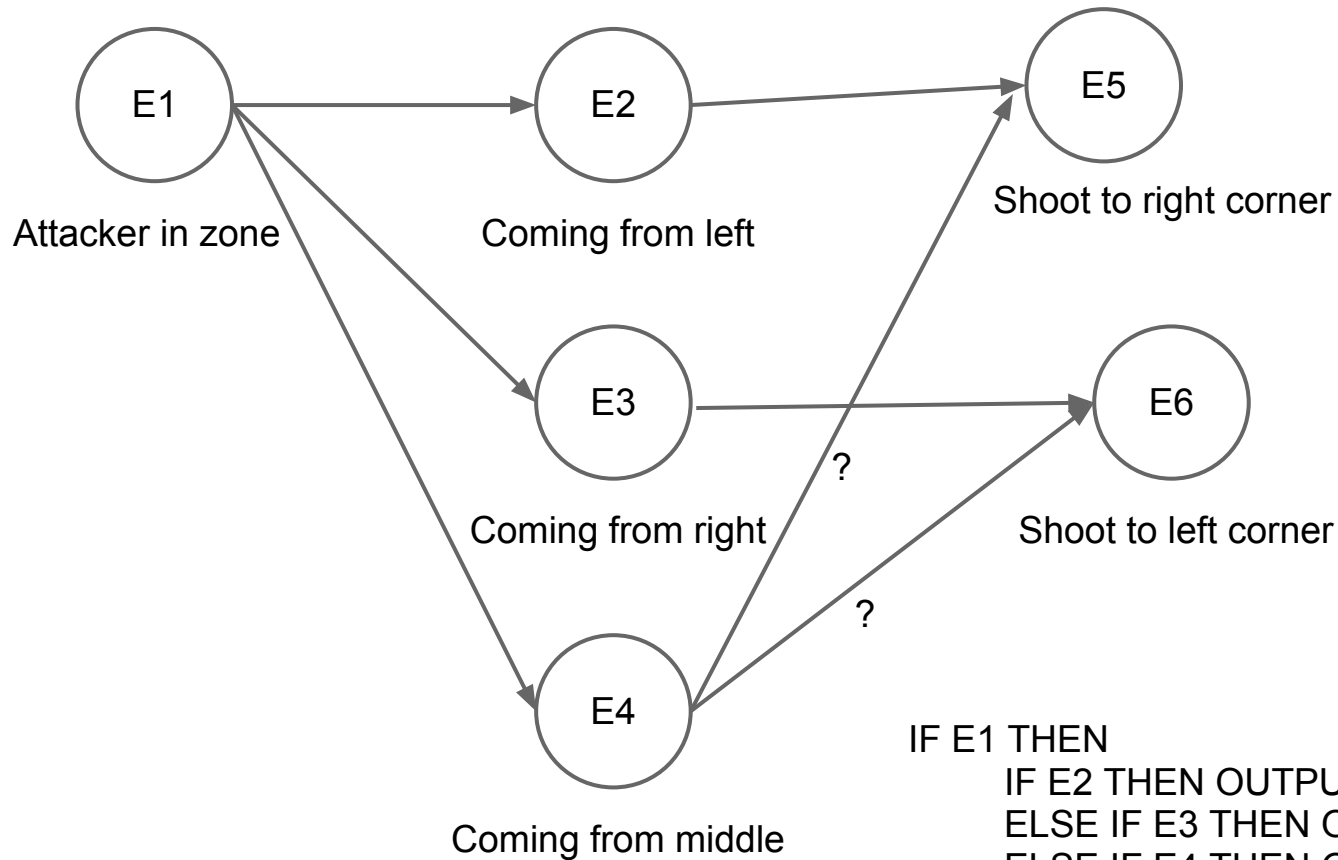


Game Artificial Intelligence by example

Evalds Urtans

Finite-state machine

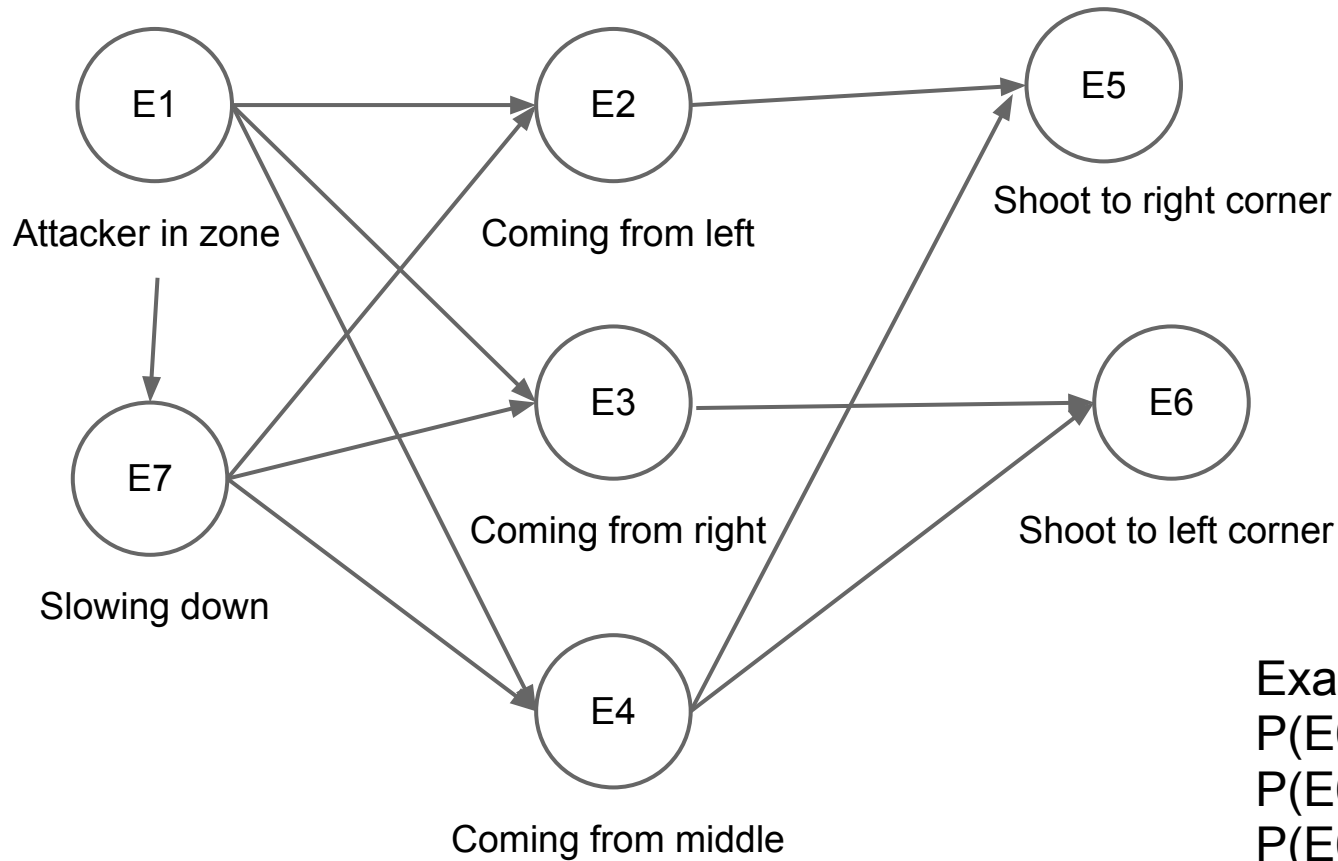
Ice Hockey game - what should goalie do?



```
IF E1 THEN
  IF E2 THEN OUTPUT = E5
  ELSE IF E3 THEN OUTPUT = E6
  ELSE IF E4 THEN OUTPUT = RAND(E5,E6)
END IF
```

Bayesian belief networks

Ice Hockey game - what should goalie do?



Example questions:

$$P(E6|E3) = ?$$

$$P(E6|E7) = ?$$

$$P(E6|E1) = ?$$

Bayesian belief networks

Ice Hockey game - what should goalie do?

Statistics (can & should be adaptive)

$P(E1)$	0.8
$P(E1, E2)$	0.4
$P(E1, E2, E3)$	0.0
$P(E1, E2, E3, E4, ..)$..
$P(E2)$	0.7
$P(E2, E1)$	0.4
$P(E2, E3)$	0.0
$P(E2, E4)$..
..	..

Bayesian belief networks

Ice Hockey game - what should goalie do?

$$P(E6|E3) = ?$$

Conditional probability (top-bottom, cause-to-effect):

$$P(E6|E3) = P(E6,E3) / P(E3)$$

Conditional probability (bottom-top, effect-to-cause):

$$P(E3|E6) = P(E6,E3) / P(E6)$$

out of this comes

Bayes rule (bottom-top, effect-to-cause):

$$P(E3|E6) = P(E6|E3) * P(E3) / P(E6)$$

Useful in problems where you have different statistical data, for example, only $P(E6|E3)$, $P(E3)$, $P(E6)$

Bayesian belief networks

Ice Hockey game - what should goalie do?

Network based statistics:

$$P(E6, E3) = 0.5$$

$$P(E3) = 0.3$$

$$P_a(E6|E3) = P(E6, E3) / P(E3) \text{ [prediction with reasoning]}$$

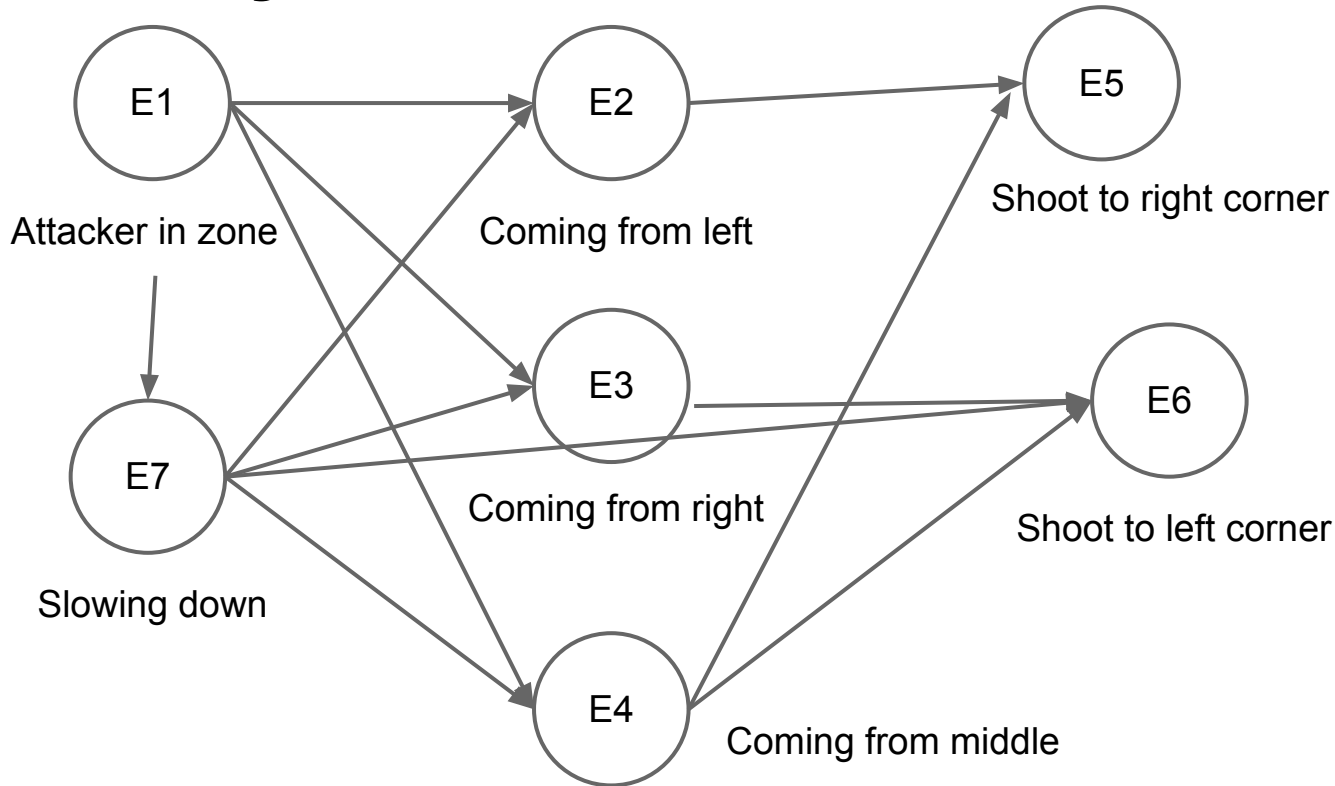
Independent statistics:

$$P_b(E6|E3) = 0.2 \text{ [prediction without reasoning]}$$

* Investigate Markov Chains model (Finite state machine /w probabilities)

$P_a(E6|E3)$ is better prediction than $P_b(E6|E3)$

Reasoning based Dempster-Shafer theory



E4 $P(E5) = 0.4$ $P(E6_1) = 0.6$

E7 $P(E2) = 0.2$ $P(E3) = 0.2$ $P(E4) = 0.5$ $P(E6_2) = 0.1$

$$P(E6_1) \neq P(E6_2) \neq P(E6)$$

Reasoning based Dempster-Shafer theory

Credibility (based on DS), Plausibility, Belief

If E4 & E7 are observed

Calculate mass of interferences between co-dependent events

$$m(E6) = P(E6_1) \cdot P(E3) + P(E6_1) \cdot P(E4) + P(E6_1) \cdot P(E6_2) = 0.6 \cdot 0.2 + 0.6 \cdot 0.5 + 0.6 \cdot 0.1 = 0.48$$

$$m(\text{not } E6) =$$

$$1 - m(E6) =$$

$$P(E5) \cdot P(E2) + P(E5) \cdot P(E3) + P(E5) \cdot P(E4) + P(E5) \cdot P(E6_2) + P(E6_1) \cdot P(E2) = 0.4 \cdot 0.2 + 0.4 \cdot 0.2 + 0.4 \cdot 0.5 + 0.4 \cdot 0.1 + 0.6 \cdot 0.2 = 0.52 \text{ (double check, not necessary)}$$

$$\text{Cedr}(E6) = m(E6) / (1 - m(E6)) = 0.92$$

$$\text{Plaus}(E6) = (P(E6_1) + P(E6_2)) / 2 = (0.6 + 0.1) / 2 = 0.35$$

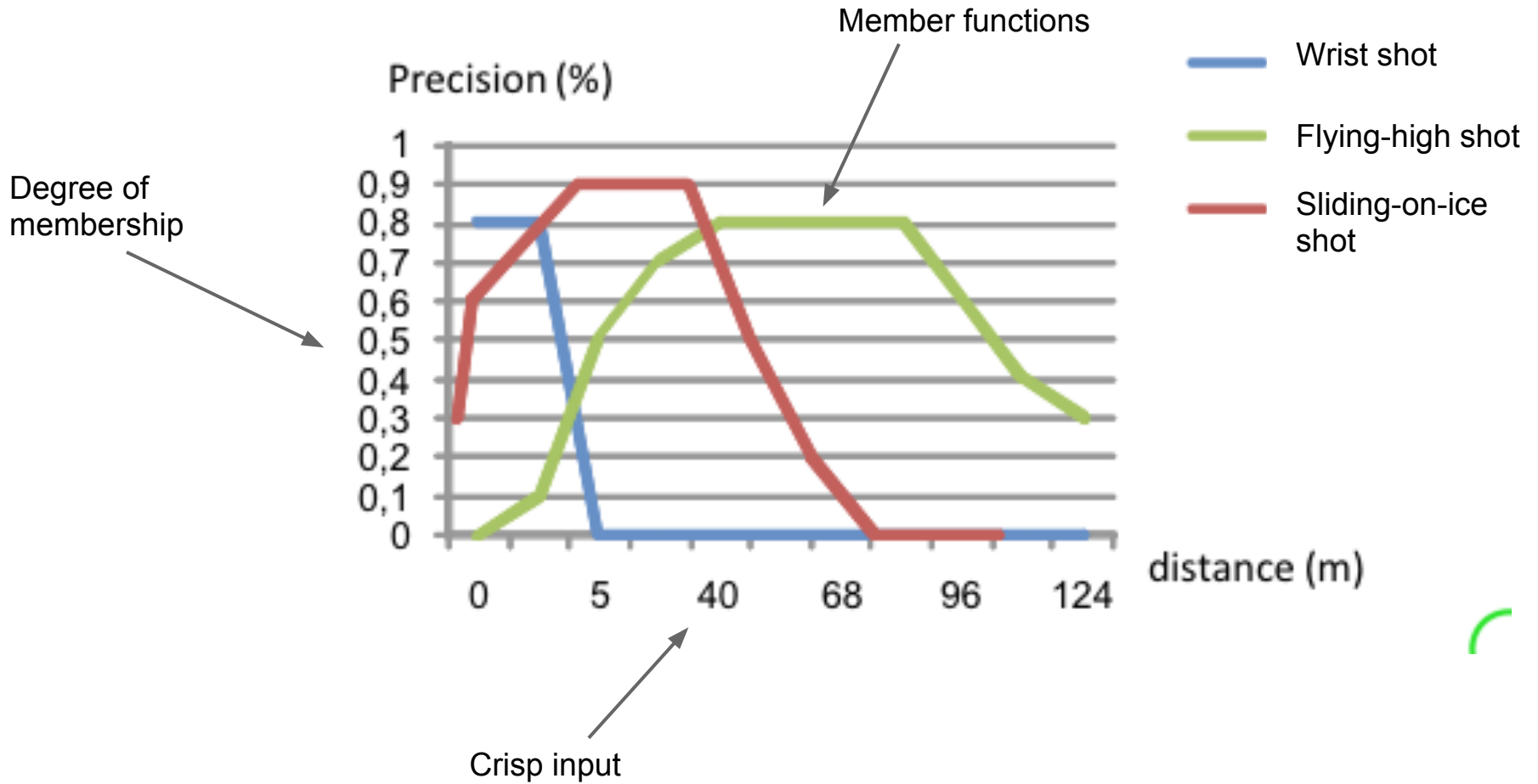
[average of all known probabilities P(E6)]

$$\text{Belief}(E6) = (\text{Cedr}(E6) + \text{Plaus}(E6)) / 2 = (0.92 + 0.35) / 2 = 0.635$$

* You can choose to be optimistic, pessimistic or rational

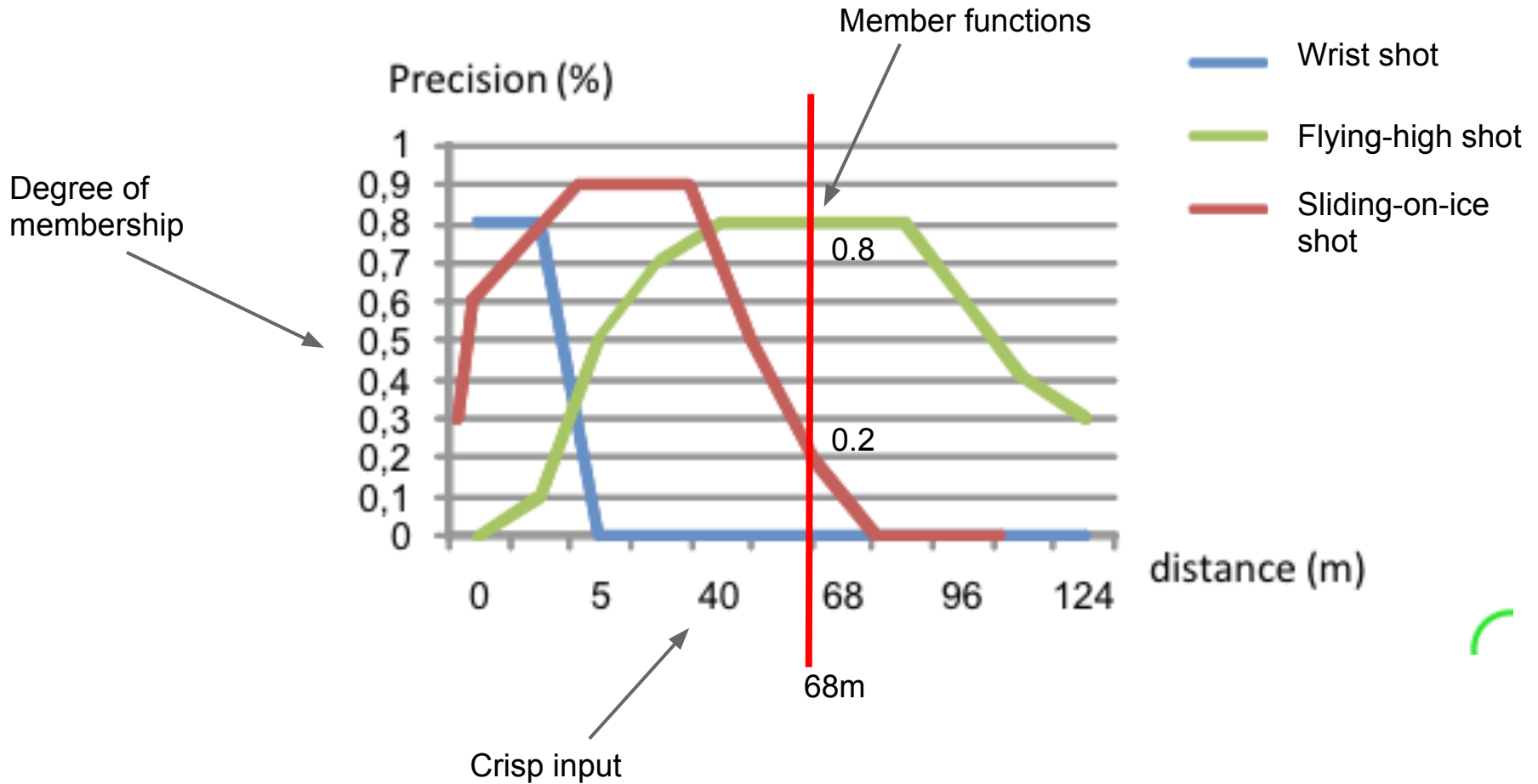
Fuzzy sets

Input = crisp value, output = degree of membership



Fuzzy sets

Input = crisp value, output = degree of membership

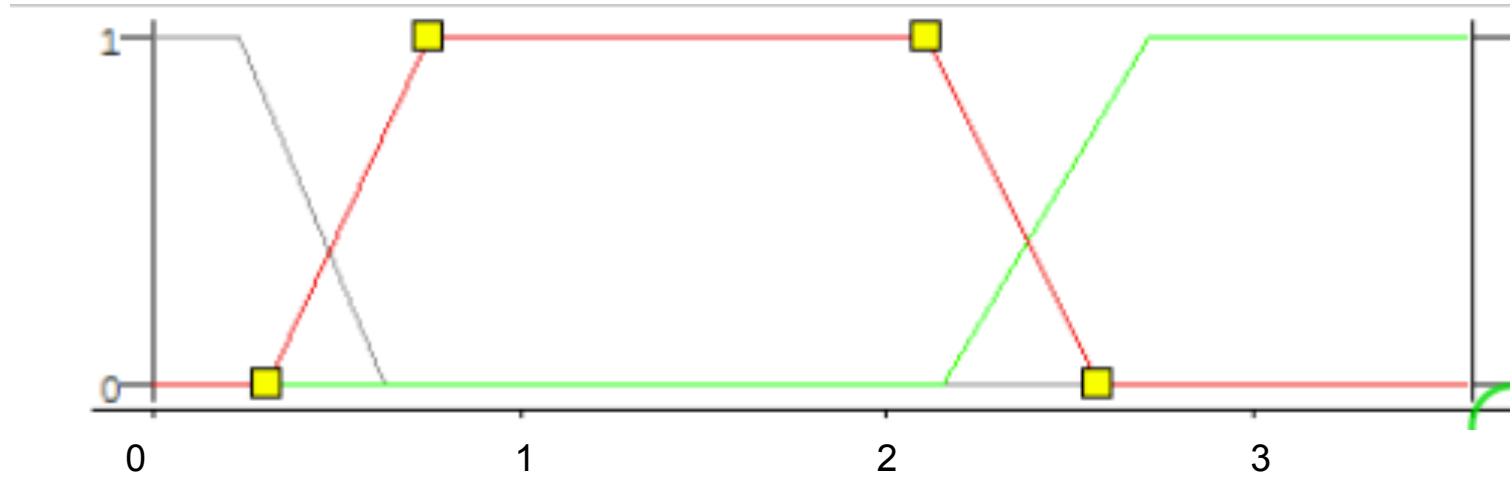


Fuzzy sets

Input = degree of membership, output = crisp value

Breakaway situation (attack close to goals):

- Goalie
- Defender
- Attacker



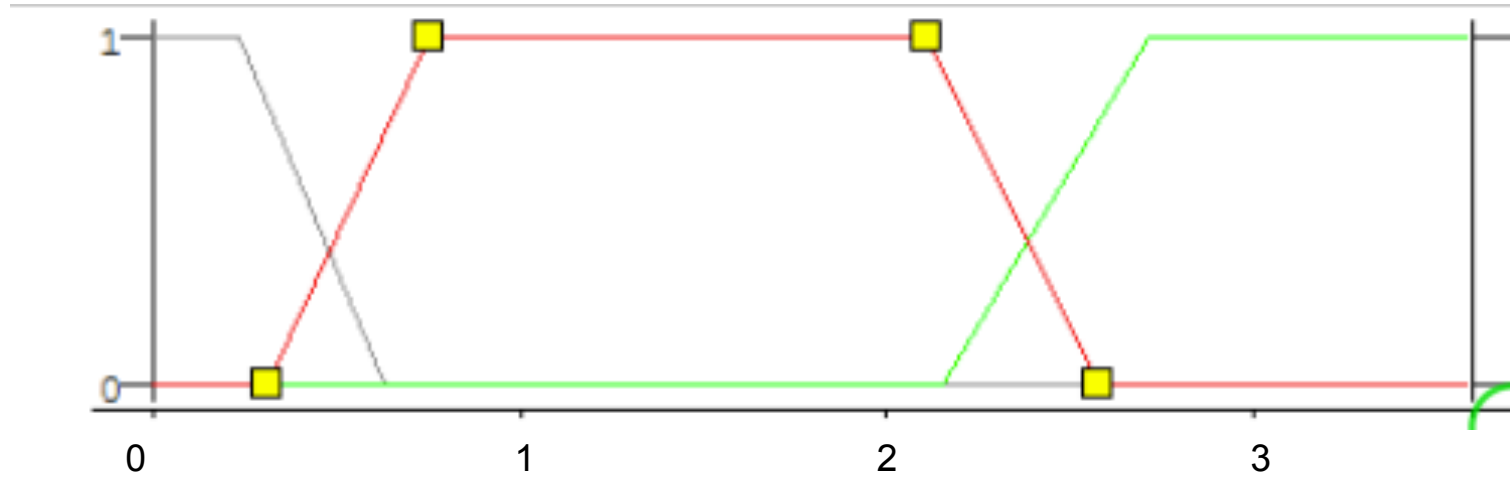
How many defenders needed to be allocated to opponent?

Fuzzy sets

Input = degree of membership, output = crisp value

Breakaway situation (attack close to goals):

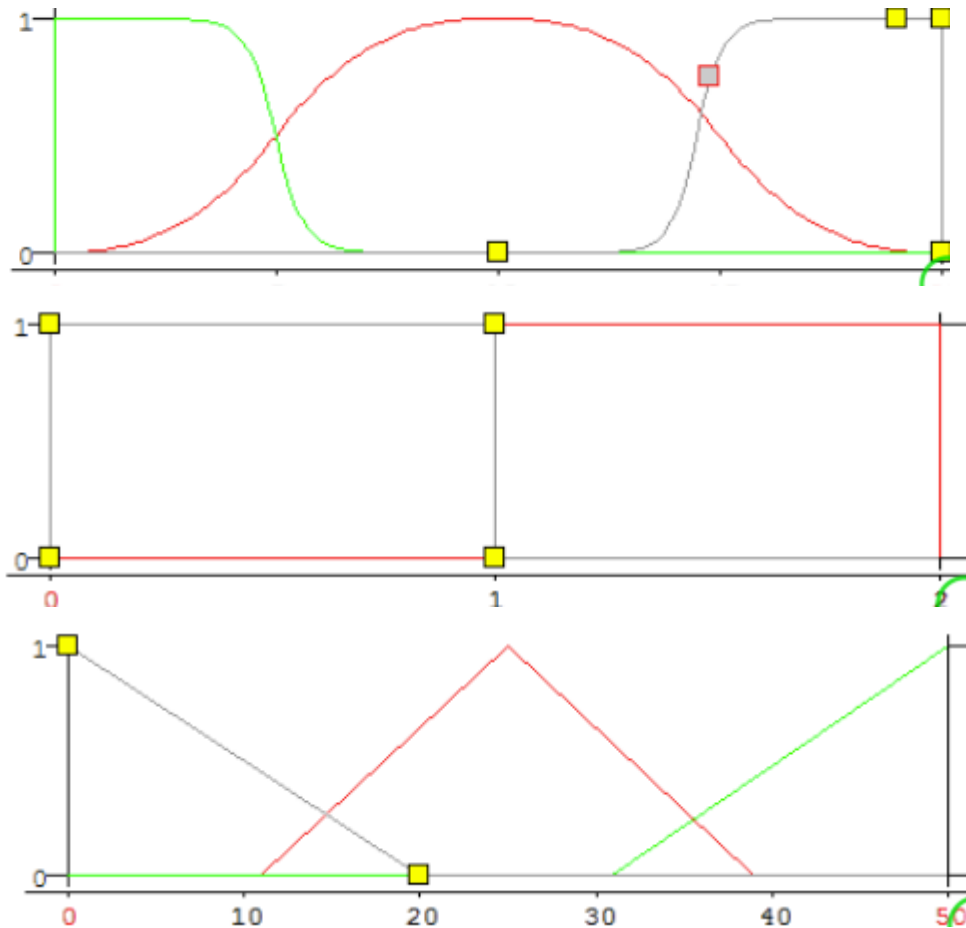
- Goalie
- Defender
- Attacker



How many defenders needed to be allocated to opponent?

Fuzzy sets

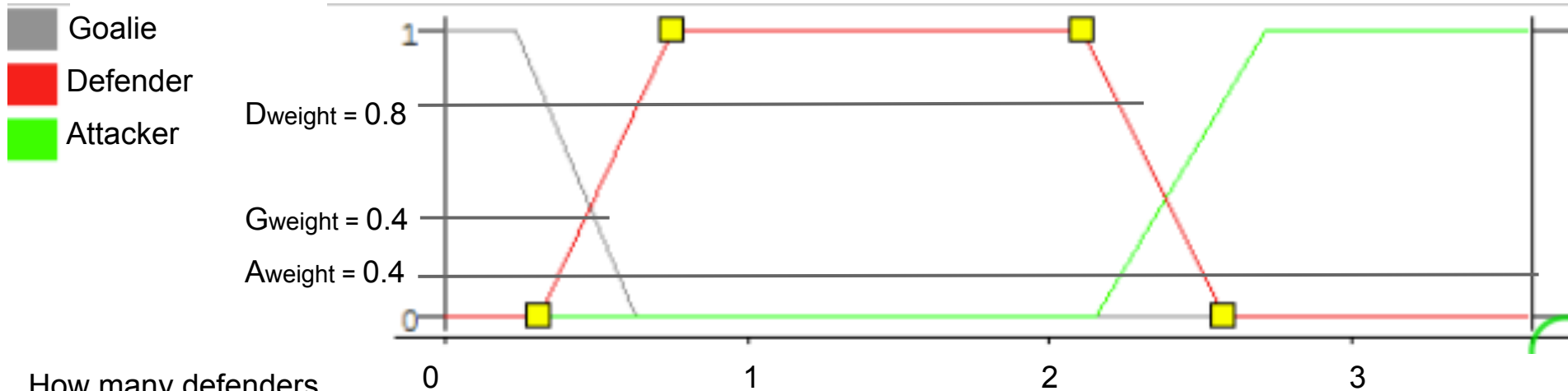
Member functions can be any geometrical function



Fuzzy sets

Input = degree of membership, output = crisp value

Breakaway situation (attack close to goals):

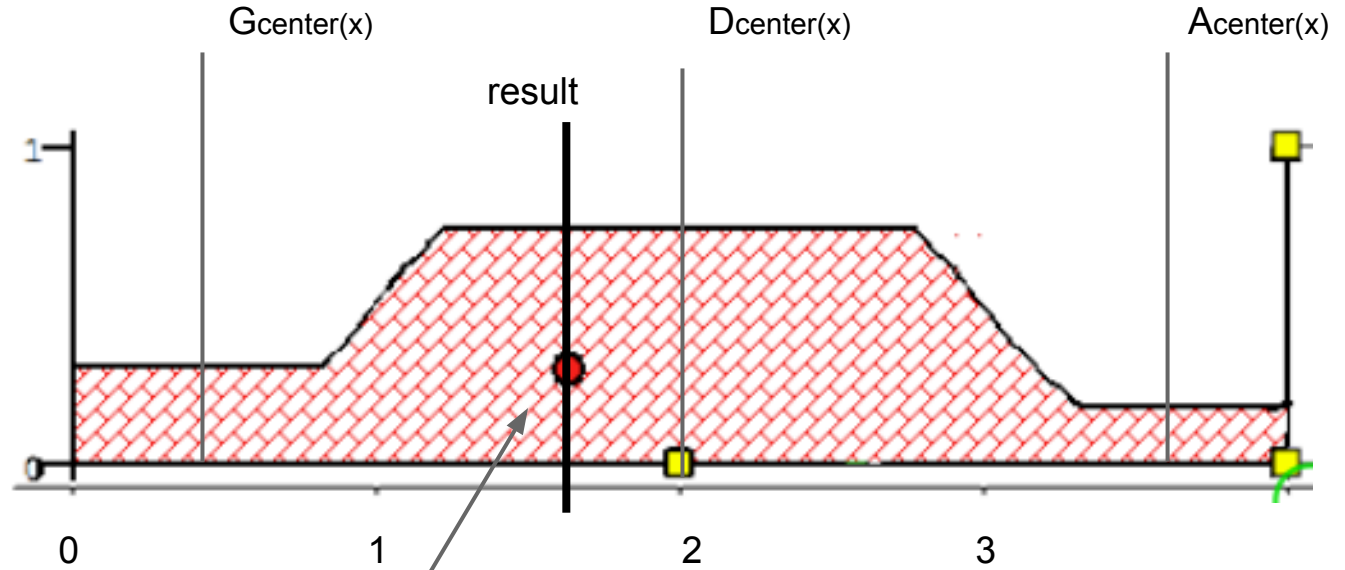


How many defenders needed to be allocated to opponent?

Fuzzification

Fuzzy sets

- Goalie
- Defender
- Attacker



How many defenders
needed to be allocated to
opponent?

Defuzzification - calculated using centroid formula (centre of mass, singleton function)

$$\text{result} = (\text{Gweight} * \text{Gcenter}(x) + \text{Dweight} * \text{Dcenter}(x) + \text{Aweight} * \text{Acenter}(x)) / (\text{Gweight} + \text{Dweight} + \text{Aweight})$$

Neural Networks

Phong game example



Figure 11 -- Ping-Pong Sample Application

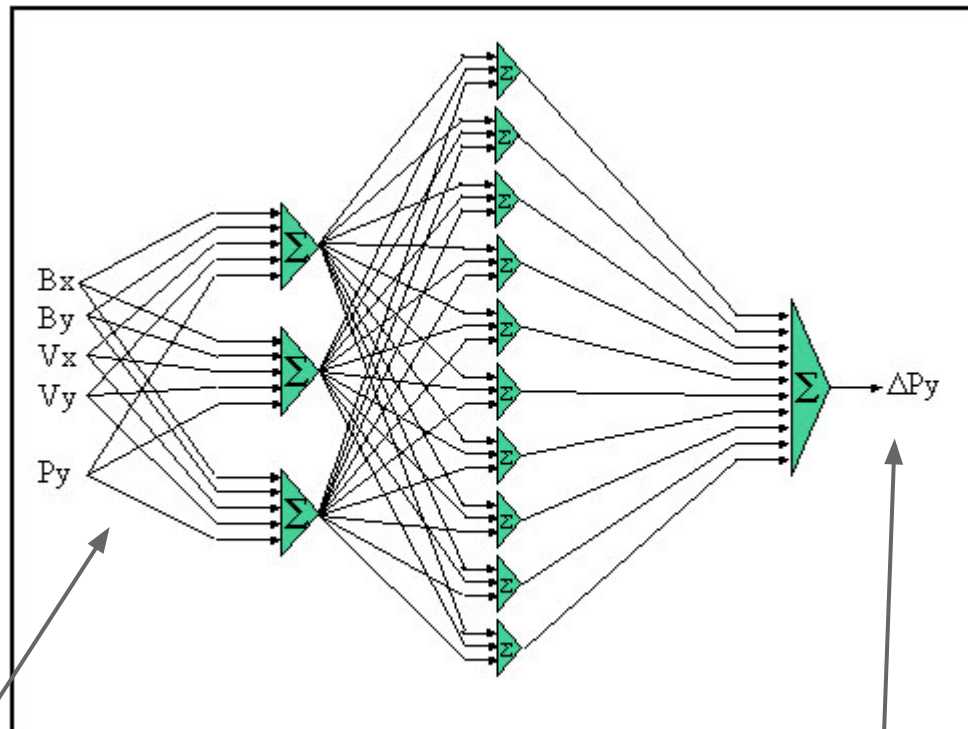


Figure 12 -- Neural Network for Ping Pong Game

Input:
Opponent's Y position,
Ball's X position,
Ball's Y position,
Ball's velocity

Output:
AI's Y position

Neural Networks

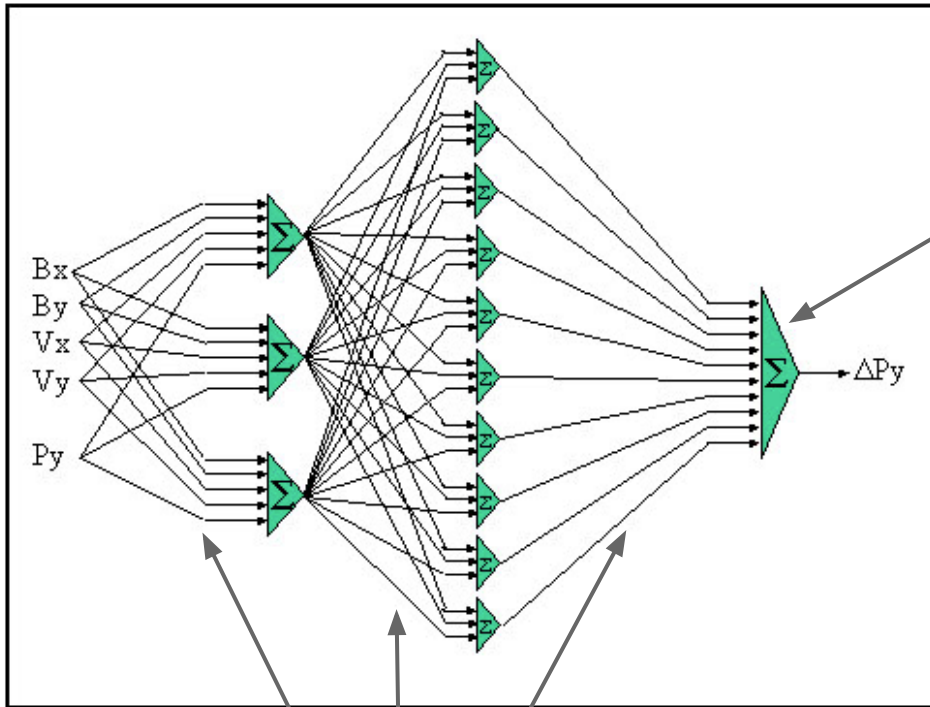
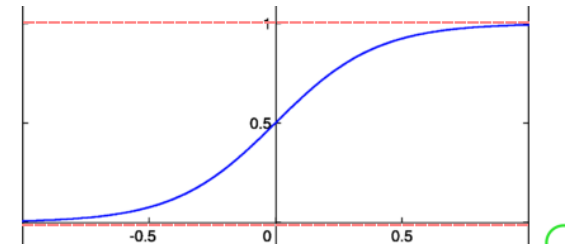


Figure 12 -- Neural Network for Ping Pong Game



Neuron resembled as sigmoid function

Weights in between connections
"connection strength between neurons"

These will change resembling a learning process (delta rule algorithm, back-propagation algorithm)

Further information

Bayesian networks

<http://www.cs.indiana.edu/classes/b351-gass/Notes/uncertainty.html>

https://controls.engin.umich.edu/wiki/index.php/Bayes_Rule,_conditional_probability,_independence

https://controls.engin.umich.edu/wiki/index.php/Bayesian_network_theory

<http://staff.utia.cas.cz/vomlel/vomlel-ova-cze-jap-2009.pdf>

http://opencourseware.kfupm.edu.sa/colleges/ccse/ics/ics381/files/2_Lectures%2030-31-Ch-14_Probabilistic%20Reasoning.pdf

<http://ai.stanford.edu/~paskin/gm-short-course/lec1.pdf>

https://controls.engin.umich.edu/wiki/index.php/Bayes_Rule,_conditional_probability,_independence

<http://www.conradyscience.com/index.php/software>

BayesiaLab - very interesting software for calculating probabilities using bayesian networks
Used in marketing research by most of the big brand companies

Further information

Dempster-Shafer theory

<http://www.google.lv/books?id=4f5Gszjyb8EC&lpg=PR11&ots=9BTKlvOwsl&dq=dempster-shafer%20game%20ai&lr&hl=lv&pg=PA356#v=onepage&q&f=false>

Neural Networks

<http://www.cs.bham.ac.uk/~jxb/NN/nn.html>

http://www.webpages.ttu.edu/dleverin/neural_network/neural_networks.html

<http://software.intel.com/en-us/articles/an-introduction-to-neural-networks-with-an-application-to-games/>

<http://www.ibm.com/developerworks/library/l-neural/>

<http://takinginitiative.net/2008/04/03/basic-neural-network-tutorial-theory/>

Further information

Fuzzy Logic

http://www.chebucto.ns.ca/Science/AIMET/archive/ddj/fuzzy_logic_in_C/

Interesting articles & research in Game-AI

<http://aigamedev.com/>